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THE MODULUS OF POLYETHYLENE

by

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#### The Modulus of Polyethylene

In a previous article in this journal, we simultaneously measured shear modulus, density, and crystallinity for linear polyethylenes as a function of temperature in samples subjected to various annealing procedures.

At sufficiently high temperatures, the degree of amorphicity becomes appreciable and the modulus becomes lower than 7 x 10 dynes/cm Under these conditions one can interpret the modulus as a rubber elasticity modulus. In the sample, under these conditions, the crystallites have a dual role: they act as crosslinks and also as filler particles. An equation has been proposed for the shear modulus:

1. 
$$G = (1-Q)dkT (1+2.5Q+14.1Q^2)$$
  
 $T m$ 

In equation (1) Q is the fractional crystallinity, d is the density, m is the molecular mass of the repeating link in the chain (CH<sub>2</sub> in this case,) k is Boltzmann's constant, T is the absolute temperature, and T is the average number of CH<sub>2</sub> units in an amorphous sequence of the polymer chain connecting two crystallites. The term in parenthesis on the right hand side is a correction for the "filler effect."

Data obtained in reference (1) on Q, d and G at various temperatures enable us to compute  $\overline{r}$ , a quantity which should be of use in characterizing crystalline polymers.

We believe that it is permissible to apply equation (1) based on rubber elasticity theory for values of G less than  $7 \times 10^8$  dynes/cm<sup>2</sup> and for values of r equal to or greater than ten. This is suggested by our systematic studies of highly crosslinked polymers<sup>3</sup>.

Table I shows the data for T, d, Q, and G for sample No. 491  $\frac{1}{M}$  =2.8x10 of reference (1) together with the values of r computed by equation (1).

It would, of course, be of great interest if other physical methods for measuring r could be developed.

Table I Linear Polyethylene

Temperature C	Density	Crystallinity	Modulus (dynes/cm <sup>2</sup> )	ī
115	0.918	0.76	6.53x10 <sup>8</sup>	10.0
. 120	0.912	0.70	4.95x10 <sup>8</sup>	14.9
125	0. 903	0. 67	3.37x10 <sup>8</sup>	22.6
130	0∘892	0.51	7.8x10 <sup>7</sup>	70.6
133	0.795	0.30	6.9x10 <sup>7</sup>	95.8

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